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**SUGGESTED SOLUTION**

**FINAL MAY 2019 EXAM**

**SUBJECT- AMA**

**Test Code – FNJ 7083**

**BRANCH - () (Date :)**

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Answer 1:

Statement Showing Standard Cost and Actual Cost of 320<sup>th</sup> Batch :

Standard Data			Actual Data			
<b>Material</b>						
<b>SQ</b>	<b>SP</b>	<b>SQ × SP</b>	<b>AQ</b>	<b>AP</b>	<b>AQ × AP</b>	<b>SP × AQ</b>
62.07 kgs.(Refer W.N. 1)	Rs. 55	Rs. 3,414	80 Kgs.	Rs. 50.00	Rs. 4,000	Rs. 4,400
<b>Labour</b>						
<b>SH</b>	<b>SR</b>	<b>SH × SR</b>	<b>AH</b>	<b>AR</b>	<b>AH × AR</b>	<b>SR × AH</b>
12.42 hours (Refer W.N.2)	Rs. 40	Rs. 497	20 hours	Rs. 50.00	Rs. 1,000	Rs. 800
<b>Variable Overhead</b>						
<b>SH</b>	<b>SR</b>	<b>SH × SR</b>	<b>AH</b>	<b>AR</b>	<b>AH × AR</b>	<b>SR × AH</b>
12.42 hours (Refer W.N.2)	Rs. 75	Rs. 932	20 hours	Rs. 90.00	Rs. 1,800	Rs. 1500

Computation of Variances :

(1 mark \* 9 = 9 marks)

**Material Cost Variance** = Standard Material Cost – Actual Material Cost

$$= SQ \times SP - AQ \times AP$$

$$= Rs. 3,414 - Rs. 4,000 = Rs. 586 (A)$$

**Material Usage Variance** = Standard Cost of Standard Quantity – Standard cost of Actual Quantity

$$= SQ \times SP - AQ \times SP$$

$$= Rs. 3,414 - Rs. 4,400 = Rs. 986 (A)$$

**Material Price Variance** = Standard Cost of Actual Quantity – Actual Material Cost

$$= AQ \times SP - AQ \times AP$$

$$= Rs. 4,400 - Rs. 4,000 = Rs. 400 (F)$$

**Labour Cost Variance** = Standard Cost of Labour – Actual Cost of Labour

$$= SH \times SR - AH \times AR$$

$$= Rs. 497 - Rs. 1,000 = Rs. 503 (A)$$

**Labour Efficiency variance** = Standard Cost of Standard Time – Standard Cost for Actual Time

$$= SH \times SR - AH \times SR$$

$$= Rs. 497 - Rs. 800 = Rs. 303 (A)$$

**Labour Rate Variance** = Standard Cost for Actual Time – Actual Cost of Labour

$$= AH \times SR - AH \times AR$$

$$= Rs. 800 - Rs. 1,000 = Rs. 200 (A)$$

**Variable Overhead Cost Variance** = Standard Variable Overheads for Production – Actual Variable Overheads

$$= \text{Rs. } 932 - \text{Rs. } 1,800 = \text{Rs. } 868(\text{A})$$

### Variable Overhead Efficiency Variance

$$= \text{Standard Variable Overheads for Production} -$$

$$\text{Budgeted Variable Overheads for Actual Hours}$$

$$= \text{Rs. } 932 - 20 \text{ Hours} \times \text{Rs. } 75$$

$$= \text{Rs. } 568 (\text{A})$$

### Variable Overhead Expenditure Variance

$$= \text{Budgeted Variable Overheads for Actual Hours} -$$

$$\text{Actual Variable Overheads}$$

$$= 20 \text{ Hours} \times \text{Rs. } 75 - \text{Rs. } 1,800$$

$$= \text{Rs. } 300 (\text{A})$$

### Working Note :

**(1) Working note showing Standard Quantity of Material for 320<sup>th</sup> Batch. (1.5 marks)**

Cumulative Number of Batches = 320

Average Kgs. of Material per batch =  $100 \times 320^{-0.074}$

$$t = 100 \times 320^{-0.074}$$

$$\log t = \log 100 - 0.074 \times \log 320$$

$$\log t = \log 100 - 0.074 \times \log (2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 5)$$

$$\log t = \log 100 - 0.074 \times [\log 2^6 + \log 5]$$

$$\log t = \log 100 - 0.074 \times [6 \log 2 + \log 5]$$

$$\log t = 2 - 0.074 \times [6 \times 0.30103 + 0.69897]$$

$$\log t = 1.81462$$

$$t = \text{Antilog } (1.81462)$$

$$t = 65.26$$

Cumulative Number of Batches = 319

Average Kgs. of Material per batch =  $100 \times 319^{-0.074}$

$$t = 100 \times 319^{-0.074}$$

$$\log t = \log 100 - 0.074 \times \log 319$$

$$\log t = \log 100 - 0.074 \times \log 319$$

$$\log t = 2 - 0.074 \times 2.50379$$

$$\log t = 1.81472$$

$$t = \text{Antilog}(1.81472)$$

$$t = 65.27$$

$$\text{Standard Quantity of Material for 320}^{\text{th}} \text{ Batch} = 320 \times 65.26 - 319 \times 65.27 = 62.07 \text{ Kgs.}$$

(2) Working note showing Standard Hours for 320<sup>th</sup> Batch. (1.5 marks)

$$\text{Cumulative Number of Batches} = 320$$

$$\text{Average Labour Hours Per batch} = 100 \times 320^{-0.322}$$

$$t = 100 \times 320^{-0.322}$$

$$\log t = \log 100 - 0.322 \times \log 320$$

$$\log t = \log 100 - 0.322 \times \log (2 \times 2 \times 2 \times 2 \times 2 \times 2 \times 5)$$

$$\log t = \log 100 - 0.322 \times [\log 2^6 + \log 5]$$

$$\log t = \log 100 - 0.322 \times [6 \log 2 + \log 5]$$

$$\log t = 2 - 0.322 \times [6 \times 0.30103 + 0.69897]$$

$$\log t = 1.19334$$

$$t = \text{Antilog}(1.19334)$$

$$t = 15.61$$

$$\text{Cumulative Number of Batches} = 319$$

$$\text{Average Labour Hours per batch} = 100 \times 319^{-0.322}$$

$$t = 100 \times 319^{-0.322}$$

$$\log t = \log 100 - 0.322 \times \log 319$$

$$\log t = 2 - 0.322 \times 2.50379$$

$$\log t = 1.19378$$

$$t = \text{Antilog}(1.19378)$$

$$t = 15.62$$

$$\text{Standard Hours for 320}^{\text{th}} \text{ Batch} = 320 \times 15.61 - 319 \times 15.62 = 12.42 \text{ hours}$$

**Answer 2:**

Dummy machine ( $X_5$ ) is inserted to make it a balanced cost matrix and assume its installation cost to be zero. Cost of install at cell  $X_3$  (P) and  $X_2$  (R) is very high marked as M.

	P	Q	R	S	T
$X_1$	18	22	30	20	22
$X_2$	24	18	M	20	18
$X_3$	M	22	28	22	14

$X_4$	28	16	24	14	16
$X_5$ (Dummy)	0	0	0	0	0

(1 mark)

**Step 1**

Subtract the minimum element of each row from each element of that row-

	P	Q	R	S	T
$X_1$	0	4	12	2	4
$X_2$	6	0	M	2	0
$X_3$	M	8	14	8	0
$X_4$	14	2	10	0	2
$X_5$ (Dummy)	0	0	0	0	0

(1 mark)

**Step 2**

Subtract the minimum element of each column from each element of that column-

	P	Q	R	S	T
$X_1$	0	4	12	2	4
$X_2$	6	0	M	2	0
$X_3$	M	8	14	8	0
$X_4$	14	2	10	0	2
$X_5$ (Dummy)	0	0	0	0	0

(1 mark)

**Step 3**

Draw lines to connect the zeros as under-

	P	Q	R	S	T
$X_1$	0	4	12	2	4
$X_2$	6	0	M	2	0
$X_3$	M	8	14	8	0
$X_4$	14	2	10	0	2
$X_5$ (Dummy)	0	0	0	0	0

There are five lines which are equal to the order of the matrix. Hence the solution is optimal. We may proceed to make the assignment as under-

	P	Q	R	S	T
$X_1$	0	4	12	2	4
$X_2$	6	0	M	2	0
$X_3$	M	8	14	8	0
$X_4$	14	2	10	0	2
$X_5$ (Dummy)	0	0	0	0	0

(1 mark)

The following is the assignment which keeps the total cost at minimum –

Machines	Location	Costs (Rs.)
X <sub>1</sub>	P	18
X <sub>2</sub>	Q	18
X <sub>3</sub>	T	14
X <sub>4</sub>	S	14
X <sub>5</sub> (Dummy)	R	0
Total		64

(1 mark)

**Answer 3:**

Let x be the number of programmes of T.V. advertising and y denote the number of programmes of radio advertising.

*Objective function:*

One T.V. programme reaches 7,50,000 customers in target audience A and 1,50,000 customers in target audience B, whereas one radio programme reaches 40,000 customers in target audience A and 2,60,000 in target audience B. Since the advertising firm desires to determine the media mix to maximise the total reach, the objective function is given by

$$\text{Maximise } Z = (7,50,000 + 1,50,000)x + (40,000 + 2,60,000)y$$

$$\text{Or } Z = 9,00,000x + 3,00,000y$$

**Condition-1:**

One programme of T.V. advertising costs Rs. 50,000 and that of Radio advertising costs Rs. 20,000. The total advertising budget is Rs.

$$2,00,000. \text{ Hence, } 50,000x + 20,000y \leq 2,00,000$$

$$\text{Or } 5x + 2y \leq 20$$

**Condition-2:**

Contract conditions require that there should be at least 3 programmes on T.V. and the number of programmes on Radio must not exceed 5.

$$\text{Therefore, } x \geq 3$$

$$y \leq 5$$

*The linear programming model for the given problem is:*

**Maximise**

$$Z = 9,00,000x + 3,00,000y$$

**Subject to the Constraints:**

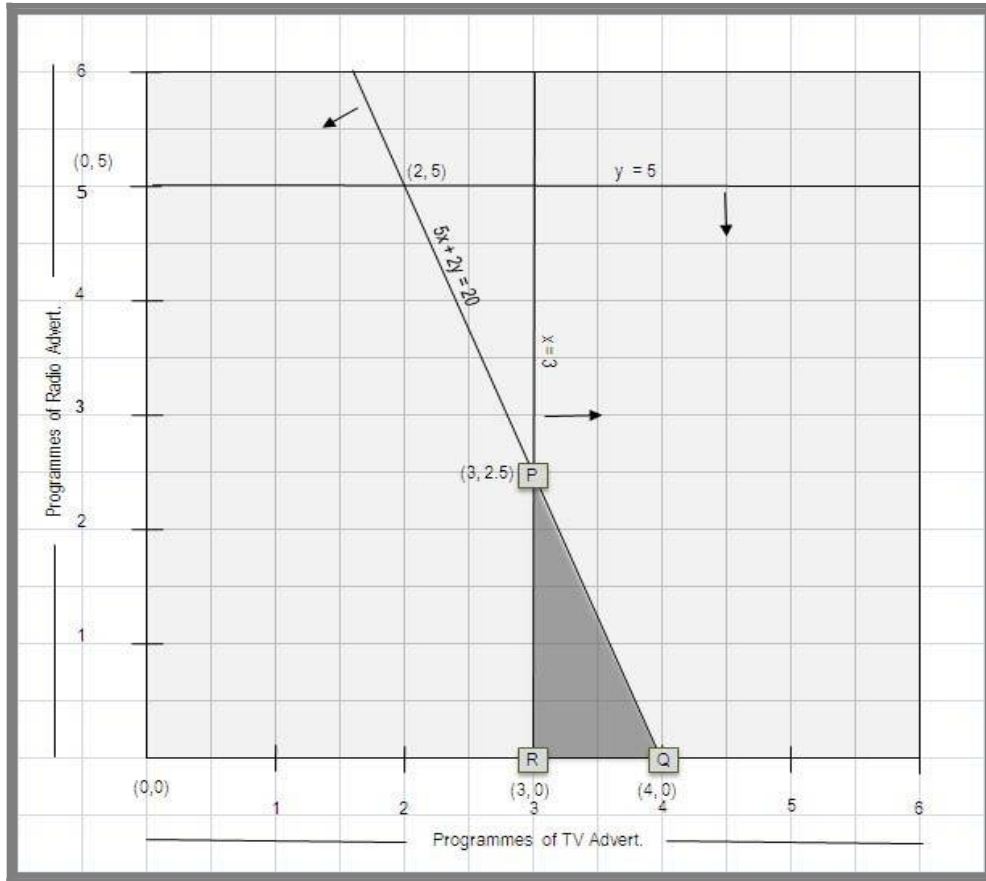
$$5x + 2y \leq 20$$

$$x \geq 3$$

$$y \leq 5$$

Where  $x, y \geq 0$

(2.5 marks)



(2.5 marks)

Answer 4:

Allocation of Random Numbers Demand (units)

(1 mark)

Units	Probability	Cumulative Probability	Random Nos.
10,000	0.20	0.20	00 – 19
20,000	0.25	0.45	20 – 44
30,000	0.30	0.75	45 – 74
40,000	0.25	1.00	75 – 99

Contribution per unit

(1 mark)

Rs.	Probability	Cumulative Probability	Random Nos.
25	0.25	0.25	00 – 24
35	0.30	0.55	25 – 54
45	0.35	0.90	55 – 89
55	0.10	1.00	90 – 99

Advertising Cost

(1 mark)

Rs.	Probability	Cumulative Probability	Random Nos.
50,000	0.22	0.22	00 – 21
60,000	0.33	0.55	22 – 54
70,000	0.44	0.99	55 – 98

80,000	0.01	1.00	99 – 99
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**Investment**

(1 mark)

Rs.	Probability	Cumulative Probability	Random Nos.
50,00,000	0.10	0.10	00 – 09
55,00,000	0.30	0.40	10 – 39
60,00,000	0.45	0.85	40 – 84
65,00,000	0.15	1.00	85 – 99

**Simulation Table**

(3 marks)

Random Number	Demand Units	Contribution Per unit (Rs.)	Adv. Cost (Rs.)	Return (Rs.)	Investment (Rs.)	Return on Investment
09, 24, 85, 07	10,000	25	70,000	1,80,000	50,00,000	3.60%
84, 38, 16, 48	40,000	35	50,000	13,50,000	60,00,000	22.50%
41, 73, 54, 57	20,000	45	60,000	8,40,000	60,00,000	14.00%
92, 07, 99, 64	40,000	25	80,000	9,20,000	60,00,000	15.33%
65, 04, 78, 72	30,000	25	70,000	6,80,000	60,00,000	11.33%

**Highest Likely Return** is 22.50% relating to trial 2.

(1 mark)

**Answer 5:**

**(a) Workings**

Activity	Duration	EST	EFT	LST	LFT	Total Float
	Dij	Ei	Ei+Dij	Lj-Dij	Lj	LST-EST
<b>A</b>	5	0	<b>5</b>	0	<b>5</b>	<b>0</b>
B	6	0	6	6	12	6
C	4	5	9	8	12	3
D	3	5	8	7	10	2
<b>E</b>	1	5	<b>6</b>	5	<b>6</b>	<b>0</b>
<b>F</b>	4	6	<b>10</b>	6	<b>10</b>	<b>0</b>
<b>G</b>	14	10	<b>24</b>	10	<b>24</b>	<b>0</b>
H	12	9	21	12	24	3
<b>I</b>	2	24	<b>26</b>	24	<b>26</b>	<b>0</b>

(3 marks)

- (i) The critical path is the series of activities within the network with *zero total float*. Accordingly, Critical Path is A–E–F–G–I with duration of 26 Days.

(1 mark)

**(ii) Project Crashing:**

Step1: Crash Activity A by 1 Day; Crashing Cost Rs. 1,000/- Step2: Crash Activity F by 1 Day; Crashing Cost Rs. 6,000/- Step3: Crash Activity G by 1 Day; Crashing Cost Rs. 7,000/-

*Activity E can not be crashed since ZERO duration is not possible.*

(1 mark)



**Requirement of Question**

**(5 marks)**

Sl. No.				
<b>(i)</b>	Duration=	26 Days		
<b>(ii)</b>	LFT:			
	C:	12		
	D:	10		
	H:	24		
	B:	12		
<b>(iii)</b>	Step	Crash Activity	Days	Cost (Rs.)
	I	A	1	1,000/-
	II	F	1	6,000/-
	III	G	1	7,000/-
<b>(iv)</b>	Activity	Increase duration by (days)		
	B	2 Days		
	C	0 Days		
<p><b>Concept:</b> B had a total float of 6 days. Due to 3 days crashing, float reduces by 3. Since B is succeeded by H, and duration of H is increased by 1, the dependent 1 float is to be reduced. Hence, float reduces by 4 days. Therefore, duration of B can be prolonged by 2 days.</p> <p>C had an original float of 3. It gained one more day due to crashing of A. It could start one day earlier. However, since it is succeeded by H, which had lost its 3 floats and increased 1 day duration, all the 4 days' float of C were consumed. Hence, no further increase in duration.</p>				

**Answer 6:**

**(i) Initial Solution by the Least Cost Method**

**(3 marks)**

	F1	F2	F3	Demand
<b>D 1</b>	3    35	6    25	7	60/25/0
<b>D 2</b>	8	5    30	7	30/0
<b>D 3</b>	4	9	11    30	30/0

<b>Supply</b>	35/ 0	55/2 0 5/	30/0	120
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<b>Supply</b>	35/ 0	55/2 0 5/	30/0	120
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- (ii) This solution is degenerate because number of occupied cells (=4) are *less than* required number (=3+3-1)

*Degeneracy is certain when in any allocation (earlier than the last allocation), the row and column totals get simultaneously fulfilled.*

In this problem, degeneracy arises as allocation at cell D1F2, *simultaneously vacates* the row and column totals. **(2 marks)**

- (iii) If we consider  $u_1 = 5$  instead of  $u_1 = 0$  for  $u_i + v_j$  matrix,  $\Delta_{ij}$  matrix would remain **same**. Since for each *occupied cell* in the table, the row value ( $u_i$ ) and column value ( $v_j$ ) equals the cost element  $C_{ij}$ . **(2 marks)**

- (iv) Initial Solution by the **North- West Corner Rule** **(3 marks)**

	F1	F2	F3	Demand
D 1	3 35	6 25	7	60/25/0
D 2	8	5 30	7	30/0
D 3	4	9	11 30	30/0
<b>Supply</b>	35/ 0	55/3 0 0/	30/0	120